

**HOME ASSIGNMENT (2025 Batch)**  
**MA/MS IN MATHEMATICS**  
**(SECOND SEMESTER)**  
**CENTRE FOR DISTANCE AND ONLINE EDUCATION**  
**DIBRUGARH UNIVERSITY**

*(Full Marks 20 for each course)*

**Course: MATH-201 (Complex Analysis)**

Assignment 1 (10)

(i).

State and prove **Cauchy's Integral Formula**. Using the formula, evaluate

$$\int_C \frac{e^z}{z-1} dz,$$

where  $C$  is the circle  $|z| = 2$ .

Assignment 2 (10)

(i)

Expand the function

$$f(z) = \frac{1}{z^2 - 1}$$

as a **Laurent series** valid in the annulus  $1 < |z| < \infty$ . Hence, classify the singularities of  $f(z)$ .

**Course: MATH-202 (Tensor)**

Assignment 1 (10)

(i)

State and prove the properties of the **Kronecker delta**. Using Kronecker delta and permutation symbol, show that

$$\epsilon_{ijk}\epsilon_{lmk} = \delta_{il}\delta_{jm} - \delta_{im}\delta_{jl}.$$

Assignment 2 (10)

(i) Explain the meaning of **covariant derivative**. Derive the expression for the divergence of a vector field in tensor notation.

**Course: MATH-203 (Differential Equations and Integral Equations)**

Assignment 1 (10)

- (i) Solve by Monge's method

$$r-2s+t = 0$$

Assignment 2 (10)

- (i) Define the **Fredholm determinant**. Explain how it is used to solve Fredholm integral equations of the second kind.

**Course: MATH-204 (Inviscid Fluid Mechanics)**

Assignment 1 (10)

- (i) Define **streamlines** and **pathlines**. Distinguish between steady and unsteady flows with examples. Derive the **equation of continuity** for a three-dimensional incompressible fluid.

Assignment 2 (10)

- (i) State and prove **Bernoulli's equation** for steady motion under conservative forces. Explain its physical significance.